

## Local and Global Properties of ODEs

\*

**Victor Edneral<sup>1</sup>, Valery Romanovski<sup>2</sup>**

We consider autonomous planar systems of ordinary differential equations with a polynomial nonlinearity. These systems are resolved with respect to derivatives and can contain free parameters. To study local integrability of the system near each stationary points, we use an approach based on Power Geometry[1] and on the computation of the resonant normal form[2, 3]. For the pair of concrete planar systems[4] and[5], we found the complete set of necessary conditions on parameters of the system for which the system is locally integrable near each stationary points. The main idea of this report is in the hypothesis that if for each fixed set of parameters such that all stationary points of the equation are centers then this system has the global first integral of motion. So from some finite set of local properties we can obtain a global property. But if the system has some invariant lines or separatists, this first integral can exist only in the part of the phase space, where center points take place.

**Keywords:** Local Integrability, Global Integrability

**Mathematics Subject Classification 2010:** 34L30, 37K10

### References

- [1] A.D. Bruno. *Power Geometry in Algebraic and Differential Equations*, Fizmatlit, Moscow, 1998 (Russian) = Elsevier Science, Amsterdam, 2000 (English).
- [2] A.D. Bruno, *Local Methods in Nonlinear Differential Equations*, Nauka, Moscow, 1979 (Russian) = Springer-Verlag, Berlin, 1989 (English).
- [3] V.F. Edneral, *On algorithm of the normal form building*, in: Ganzha et al. (Eds.) Proceedings of the CASC 2007, Springer-Verlag series: LNCS 4770 (2007) 134–142.
- [4] A. Algaba, E. Gamero, C. Garcia, The integrability problem for a class of planar systems, *Nonlinearity* v. 22 (2009) 395–420
- [5] V.A. Lunkevich, K.S. Sibirskii, *Integrals of General Differential System at the Case of Center. Differential Equation*, v. 18, No 5 (1982) 786–792 (Russian).

---

\*The publication has been prepared with the support of the "RUDN University Program 5-100" and funded by RFBR according to the research projects No. 12-34-56789 and No. 12-34-56789. Valery Romanovski acknowledges the financial support from the Slovenian Research Agency (research core funding No. P1-0306 and project N1-0063).

<sup>1</sup>Peoples' Friendship University of Russia (RUDN University)  
6 Miklukho-Maklaya st., Moscow, 117198, Russian Federation

Skobeltsyn Institute of Nuclear Physics  
Lomonosov Moscow State University  
Leninskie Gory 1(2), Moscow, 119991, Russian Federation  
edneral\_vf@pfur.ru

<sup>2</sup>Faculty of Electrical Engineering and Computer Science  
University of Maribor  
Koroška cesta 46, Maribor, SI-2000 Maribor,

CAMTP – Center for Applied Mathematics and Theoretical Physics  
University of Maribor  
Mladinska 3, Maribor SI-2000

Faculty of Natural Science and Mathematics  
University of Maribor  
Koroška cesta 160, SI-2000 Maribor, Slovenia  
valery.romanovsky@uni-mb.si